**Measuring environmental inefficiency through machine learning: An approach based on Efficiency Analysis Trees and by-production technology**

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**MATHEMATICAL MODELS**

**By-production DEA**



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**By-production FDH**





**By-production EAT**





**By-production CEAT**



